

International Journal of Innovative Research in Electrical, Electronics, Instrumentation and Control Engineering

ISO 3297:2007 Certified

Vol. 5, Issue 3, March 2017

A Study on System Reliability in Weibull Distribution

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Abstract: This paper presented the estimation of system reliability using two parameter Weibull distribution. The parameters are estimated using Weibull probability plot & statistical analysis and the results being presented in charts. An increasing complexity of systems often leads to an increase of failure mechanisms. A statistical analysis of the lifetime of systems with several failure mechanisms consisting of several subcomponents considered The Weibull distribution is commonly used as a lifetime distribution in reliability applications. The two-parameter Weibull distribution can represent a decreasing, constant or increasing failure rate.

Keywords: Reliability, Weibull distribution, WPP Method. MSC Code: 62EXX.

1. INTRODUCTION

Weibull distribution is named after Walodi Weibull (1887 estimators which have smallest mean square error [4]. – 1979). It is very flexible and can through an appropriate choice of parameters and model many types of failure rate behaviors. This distribution can be found with two or three parameters; scale, shape and location parameters. There are a number of methods for estimating the values of these parameters; some are graphical and others are analytical. Graphical methods include Weibull probability plotting is used for the reliability analysis & the Pareto analysis is and hazard plot. These methods are not very accurate but they are relatively fast. The analytical methods include maximum likelihood method, least square method and method of moments. These methods are considered as more accurate and reliable compared to the graphical method. In this article an attempt is made to estimate the system reliability using two parameter Weibull distributions & Computation is made using 'Windchill quality solution 10.2 Tryout' Software. The Maximum likelihood and median rank regression methods are used by researchers to estimate parameters of Weibull distribution [1]. Parameter estimation method for the machine tool reliability analysis to overcome the problem of unavailability of a well-defined failure data collection mechanism was given by Lad et al.[2]. It uses the knowledge and experience of maintenance personnel to obtain the parameters of lifetime distribution of the repairable as well as non-repairable components subassemblies.

The Weibull distribution is the standard function used by the wind energy community to model the wind speed frequency distribution and compare the methods [3]. Estimation the reliability function using the Maximum likelihood Method & Weighted Least Square Method & simulation procedure using Monte Carlo Method are used and several experiments are implemented to find the best

Monte Carlo simulations are used to investigate the correlation between system complexity and component lifetime distributions. [5].Moments, maximum likelihood and least squares are compared & used the means square error & total deviation, as measurement for the comparison between these methods [6]. Weibull technique carried out. The spare parts optimization was also carried out for a few vital components of this wind farm and the results are presented [7]. Gear box assembly analysis and the failure data in various operating conditions was taken from the logbooks of the vehicles. For modeling purposes the Weibull distribution has been chosen & result will be useful to the maintenance engineer to find the unreliability of the gear box assemblies and also for future strategic decision making [8]. Paritosh Bhattacharya presented the analytical methods for estimation of parameters [9]. Reliability analysis of fans using Weibull and lognormal models & analyze the current test design of fans [10]. The comprehensive analysis for complete failure data using Weibull Distribution and the Median rank regression (MRR) for data- fitting method is described and goodnessof-fit using correlation coefficient [11]. Analyses of real data set & compare these estimators in terms of deficiency via Monte Carlo simulation [12]. The moment-based piecewise polynomial model are proposed to estimate the parameters of the reliability & probability distribution of the products [13]. The shape and scale parameters of the distribution are frequently used to design and characterize commercial wind conversion machines, examine three models [14]. Two parameter different Weibull distribution's linear regression model is used for analyzing wind speed pattern variations. [15].



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2. METHODS

2.1 Weibull Distribution

The two parameter Weibull distribution requires characteristic life (η) and shape factor (β) values. Beta (β) determines the shape of the distribution. If β is greater than 1, the failure rate is increasing. If β is less than 1, the The y-axis is slightly more complicated, since it must failure rate is decreasing. If β is equal to 1, the failure rate represent is constant. There are several ways to check whether data follows a Weibull distribution, the best choice is to use a Weibull analysis software product. If such a tool is not available, data can be manually plotted on a Weibull probability plot to determine if it follows a straight line. A straight line on the probability plot indicates that the data is following a Weibull distribution. Weibull shape parameter β also indicates whether the failure rate is constant or increasing or decreasing if $\beta = 1.0$, $\beta > 1.0$, β <1.0 respectively. The cumulative % failures versus operating time data are plotted on Weibull graph [10, 11] Fig. (1, 2,3,4,5 & 6) and the values of the parameters are obtained using the statistical software 'Windchill quality solution 10.2 Tryout' software.

2.2 Weibull Probability Plotting

A distribution's probability plotting paper is constructed by linear the cumulative density function (CDF) or unreliability function of the distribution. Once this has occurred, the scales for the x- and y-axis of the distribution's plotting paper can be constructed. The CDF or unreliability function [6] of the two-parameter Weibull distribution is given by equation (1)

$$F(t) = Q(t) = 1 - e^{-\left(\frac{t}{\eta}\right)^p}$$
(1)

Where

 β & η are scale & shape parameters.

The equation (1) may be written in linear form as follows Y = mx + c(2)

$$Q(t) = 1 - e^{-\left(\frac{t}{\eta}\right)^{\beta}}$$
$$\ln(1 - Q(t)) = \ln\left(e^{-\left(\frac{t}{\eta}\right)^{\beta}}\right)$$
$$\ln(1 - Q(t)) = -\left(\frac{t}{\eta}\right)$$
$$\ln(-\ln(1 - Q(t))) = \beta \ln\left(\frac{t}{\eta}\right)$$
$$\ln\left[-\ln\left(\frac{1}{1 - Q(t)}\right)\right] = \beta \ln t - \beta \ln \eta$$
$$y = \ln\left[\ln\left(\frac{1}{1 - Q(t)}\right)\right]$$
$$X = \ln(t)$$

The CDF equation can now be rewritten as: $y=\beta x-\beta \ln(\eta)$ This is now a linear equation, with a slope of β and an intercept of $\beta \ln(\eta)$. Now the x- and y-axes of the Weibull probability plotting paper can be constructed. The x-axis is simply logarithmic, since x=ln(t)

$$y = \ln\left[\ln\left(\frac{1}{1 - Q(t)}\right)\right]$$

Reliability is defined as the probability in which an item or an entity performs its intended function over a period of time understated conditions. The reliability function for the two-parameter Weibull distribution is given as.

$$R(t) = e^{-\left(\frac{t}{\eta}\right)^{\beta}}$$
(3)

The Weibull failure rate function is defined as the number of failures per unit time that can be expected to occur for the product. It is given as.

$$\lambda(t) = \frac{\beta}{\eta} \times \left(\frac{t}{\eta}\right)^{\beta - 1} \tag{4}$$

The two-parameter Weibull probability density function f(t) is given as

$$PDF = f(t) = \frac{\beta}{\eta} \times \left(\frac{t}{\eta}\right)^{\beta-1} \times e^{-\left(\frac{t}{\eta}\right)^{\beta}}$$
(5)

$$CDF = F(t) = 1 - \left(\frac{t}{\eta}\right)^{\beta}$$
(6)

The mean life or mean time of failure (MTTF or MTBF) is defined as the average time of failure-free operation up to a failure event calculated from a homogeneous lot of equipments under operation. The MTTF or MTBF of the Weibull PDF is given as

$$MTBF = E(T) = \gamma + \eta \times \Gamma\left(\frac{1}{\beta} + 1\right)$$
(7)

3. CASE STUDY

Estimation of reliability, failure rate failure density (PDF) cumulative density function & unreliability of diesel engine for compressor application of twenty four same Make & Model the time to failure of cooling system the failure data as given below

1576,1220,1435,2154,1987,2870,2740,2847,1400,2417,21 76,1933,2966,1856,2770,1550,2195,2805,1195,604,425, 908.1745.1345.

DOI 10.17148/IJIREEICE.2017.5308



International Journal of Innovative Research in Electrical, Electronics, Instrumentation and Control Engineering ISO 3297:2007 Certified

Vol. 5, Issue 3, March 2017

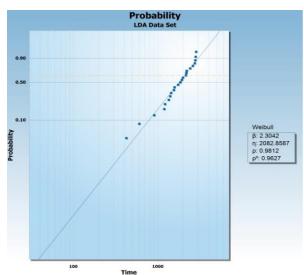
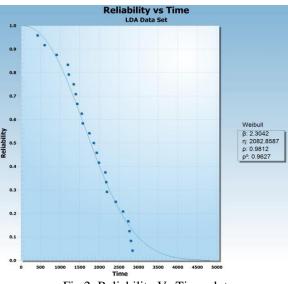
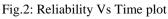


Fig.1: Weibull probability plot





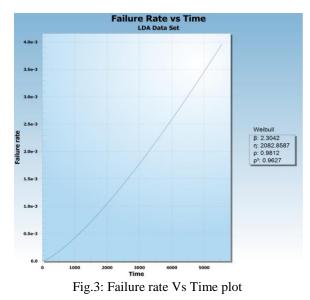




Fig.4: Unreliability Vs Time plot

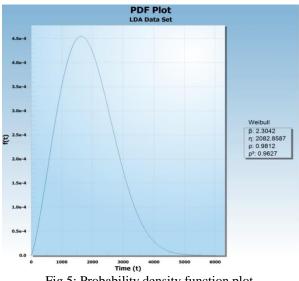


Fig.5: Probability density function plot

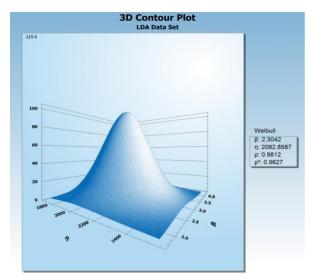


Fig.6: 3D Contour plot

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Using the software tool 'Windchill quality solution 10.2 nature from overloading the engine and fatigue of Tryout' the Weibull parameters are: material, to wear and corrosion, it was necessary to

 β = 2.3042 η = 2082.8587 ρ = 0.9812 ρ 2 =0.9627

Estimation of Mean time between failure (MTBF) or subsystems (parts) and their contribution to overall Expected time to system failure E (T) reliability and failure rate.

MTBF =E(T)=
$$\gamma + \eta \times \Gamma\left(\frac{1}{\beta} + 1\right) = 0 + 2082.8587 \times \Gamma$$

 $(1/2.3042 + 1) = 2082.8587 \times \Gamma (1.434)$ = 1845.49 hours

Reliability = $R(t) = e^{-\left(\frac{t}{\eta}\right)^{\beta}} = e^{-\left(\frac{184549}{20828587}\right)^{2.3042}} = 0.469$

Cumulative density function = CDF = F(t)=1-e^{-\left(\frac{t}{\eta}\right)^{\beta}} = 1-0.469 = 0.53

Failure
$$\operatorname{rate} = \lambda(t) = \frac{\beta}{\eta} \times \left(\frac{t}{\eta}\right)^{\beta - 1}$$

$$=\frac{2.3042}{2082.8587} \times \left(\frac{1845.49}{2082.8587}\right)^{2.3042-1} = 9.45 \times 10^{-4}$$

Probability density function = PDF= R (t) $\times \lambda$ (t) = 0.469 \times [7] 9.45 x 10⁻⁴ = 4.31 \times 10⁻⁴

Weibull distribution parameters are estimated using 'Windchill quality solution 10.2 Tryout' software tool very easily and statistical computation & charts are presented in fig (1, 2,3,4,5, and 6) the Fig 1. Presented the Weibull probability plot with parameters are estimated & failure pattern of diesel engine. Fig 2 presents the reliability of diesel engine using failure data. Fig. 3 shows the failure rate but failure rate is not constant due to repairable system it may increase, constant or decreasing. Fig 4 shows unreliability vs time plot of diesel engine. Fig 5 shows probability density function on basis of time to failure of diesel engine & Fig. 6 shows the 3D contour plot .In present case study electric & electronics system & components are not considered which may be analyzed based on similar basis with different Weibull parameters.

4. CONCLUSION

We conclude that conducted research regarding the Weibull parameter estimation using 'Windchill quality solution 10.2 Tryout' software and estimation of the reliability of diesel engine, the parameter estimation is very fast as compared to the analytical methods. As per literature survey this method is not accurate but relatively fast. The empirical approximation of functions was taken and it showed that the Weibull distribution parameters are $\beta = 2.3042$ and $\eta = 2082.8587$ approximates well the reliability of the diesel engine, and that the expected time of failure-free function E (T) = 1845.49h. Starting from the established fact that diesel engine has an increasing rate of failure, and that failure causes may be different in

nature from overloading the engine and fatigue of material, to wear and corrosion, it was necessary to determine the individual failure rates of diesel engine subsystems (parts) and their contribution to overall reliability and failure rate.

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